



### 3. SIMULATION GEOMETRY, RESULTS, AND DISCUSSION

In the numerical electromagnetic simulations, we studied the effect of the waveguide material on the ‘waveguide to sphere coupling’ by changing the material of the slab waveguide, exciting the sapphire microdisk. The slab waveguide was coupled to a sapphire microdisk with a radius of  $a = 1.5 \mu\text{m}$  and refractive index 1.764. The excitation wavelength was set in the near-IR region from 795 nm to 855 nm. Four different materials were used in the waveguide: glass with a refractive index of 1.455, sapphire with a refractive index of 1.764, diamond with a refractive index of 2.419, and silicon with a refractive index of 3.681. The excitation beam was placed at an impact parameter of  $b = 1.9 \mu\text{m}$ . The width of the waveguide  $w = 400 \text{ nm}$  was chosen such that, the waveguide would be single mode for operation at 800 nm for the case of glass, sapphire, and diamond. Ideally, the waveguide should have both a core and a cladding for evanescent coupling to the microdisk. The radial mode order  $l$ , and the angular mode number  $n$  will be specified for each numerical simulation. By changing the impact parameter  $b$  or the wavelength  $\lambda$ , it is possible to address various mode orders  $l$  or mode numbers  $n$ . The mode spacing is given by  $\lambda^2/2a\pi m = 43.5 \text{ nm}$  at 850 nm and 38.5 nm at 800 nm. The excitation from the left port of the waveguide is in the  $z$  direction (perpendicular to the paper) and the following figures show the electric field (perpendicular to the paper) strength everywhere in the  $xy$  plane.

Figure 2 shows off/on resonance condition for sapphire microdisk coupled to a glass waveguide. The off-resonance wavelength is at 819 nm, while the on resonance wavelength is at 800 nm. For the on resonance case the angular mode number is  $n = 17$  and radial mode order is  $l = 1$ . Figure 3 shows the off/on-resonance condition for sapphire microdisk coupled to a sapphire waveguide. The off-resonance wavelength is 820.6 nm, while the on-resonance wavelength is 795.6 nm. For the on-

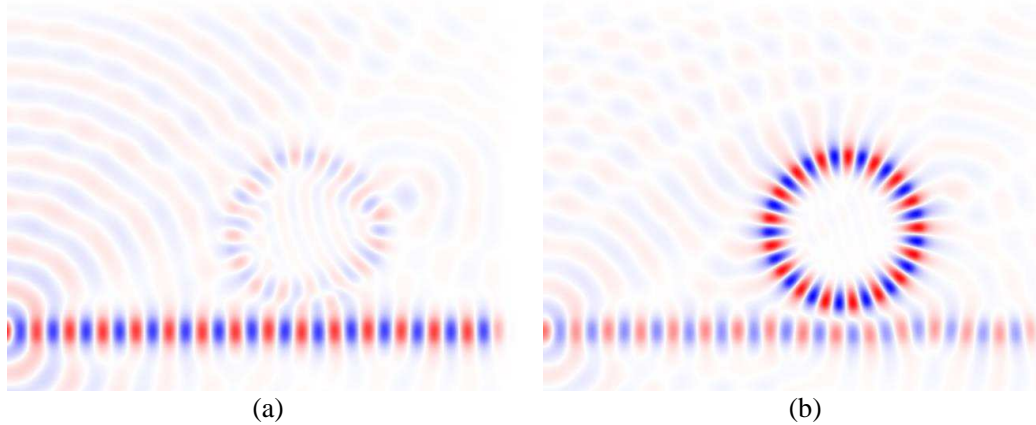


Figure 2: (a) The off-resonance at 819 nm and (b) on-resonance at 800 nm excitation for sapphire microdisk on glass slab waveguide.

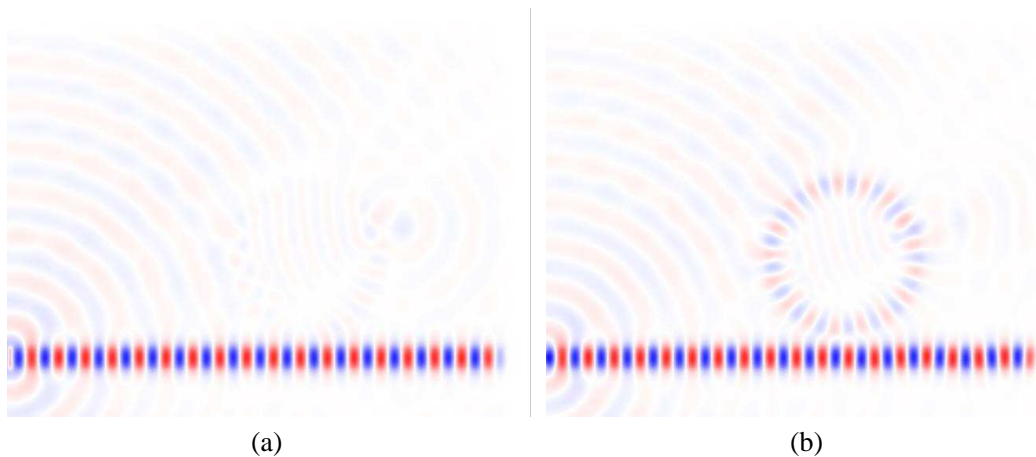


Figure 3: (a) The off-resonance at 820.6 nm and (b) on-resonance at 795.6 nm sapphire microdisk on sapphire slab waveguide excitation.

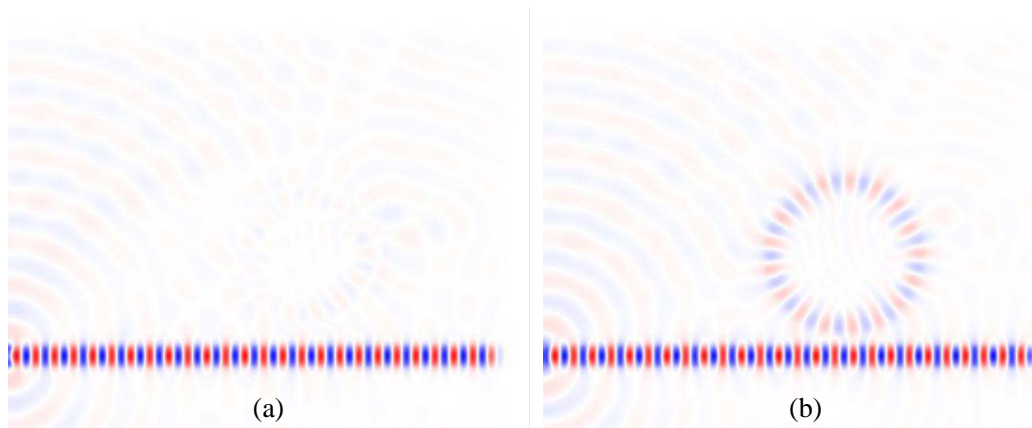


Figure 4: (a) The off-resonance at 820 nm and (b) on-resonance at 799.6 nm sapphire microdisk on diamond slab waveguide excitation.

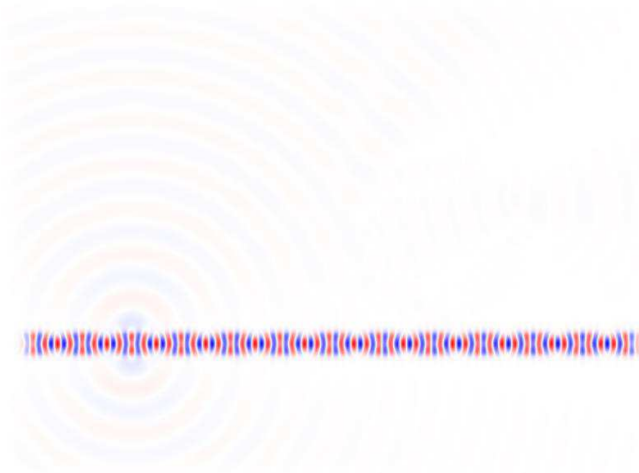


Figure 5: Sapphire microdisk on silicon slab waveguide at a wavelength of 800 nm. There is no evanescent excitation to the microdisk.

resonance case the angular mode number is  $n = 17$  and radial mode order is  $l = 1$ . Figure 4 shows the off/on-resonance condition for sapphire microdisk on a diamond waveguide. The off-resonance wavelength is 820 nm, while the on-resonance wavelength is 799.6 nm. For the on-resonance case the angular mode number is again  $n = 17$  and radial mode order is  $l = 1$ . Figure 5 shows the excitation of sapphire microdisk by a silicon slab waveguide excited with a wavelength of 800 nm. As the refractive index of silicon is bigger than sapphire, there is no appreciable evanescent coupling from the waveguide to the sapphire microdisk.

#### 4. CONCLUSIONS

We have shown that the sapphire microdisks can be used as optical resonators, which eventually can be used for applications such as biosensing, and optical communication. We demonstrated our approach by numerically calculating the electric field strengths of an evanescently coupled sapphire microdisk (the 2D analogue of the sapphire microsphere) and various slab waveguides (the 2D analogue of the optical waveguide) of glass, sapphire, diamond, and silicon. As the refractive index of silicon is higher than sapphire, there is no significant evanescent coupling from the silicon waveguide to the sapphire microdisk.

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